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1 Question 1

1.1 Question

Given the following code, what is the return value of `bar(24)`?

```c
#include <stdio.h>

void bar(int n){
    if(n<=2) return;
    if(n%2 == 0)
        printf("B");
    else{
        printf("A");
    }
    bar(n/2 + ((n+1*2%3 == 0) ? 1 : 0));
}

int main(){
    bar(24);
    return 0;
}
```

1.2 Answers

(A) BABA
(B) ABA
(C) BBBA
(D) BBBB
(E) Stack overflow

1.3 Proposed solution

The correct answer is (C) BBBA.

The function `bar` prints “A” if its argument is odd and “B” otherwise, then it calls itself until the argument is at most 2.

Let us analyze what the argument will be when `bar` calls itself. The piece of code is:

```c
bar(n/2 + ((n+1*2%3 == 0) ? 1 : 0));
```

Since the multiplication and the modulo operator have the same precedence, and both are executed before the addition, the ternary operator will return 1 only if `n+2` is zero. Therefore the calls to `bar` will be the following:

- `bar(24)` which prints “B”;
- `bar(12)` which prints “B”;
- `bar(6)` which prints “B”;
- `bar(3)` which prints “A”;
- `bar(1)` which returns, since its argument is less than 2.
2 Question 2

2.1 Question

Given the following code, what does the program print?

```c
#include <stdio.h>

void foo(int** a){
    int i;
    for(i=0; i<3; i++)
        (*a)++;
}

void bar(int* a){
    foo(&a);
    printf("%d\n", *(a+1));
}

int main(){
    int data[4] = {1,2,3,4};
    bar(data);
    return 0;
}
```

2.2 Answers

(A) 1
(B) 2
(C) 4
(D) Cannot tell: the behavior of the program is undefined

2.3 Proposed solution

The correct answer is (D) Cannot tell: the behavior of the program is undefined.

The function `foo` modifies the pointer `*a` incrementing it 3 times. The function `bar` calls the function `foo`, making `a` pointing to the third integer in memory next to the original one, then it prints the next integer (the fifth one in the original array).

Since `data` inside the `main` function is 4 elements long, `bar` is reading out of the bounds of the array, leading to an undefined behaviour.
3 Question 3

3.1 Question
How would you declare in C a “pointer x to an array of 10 pointers to a function that takes one int and returns a pointer to void”?

3.2 Answers
(A) void* (**x[10])(int)
(B) void* (*(*x)[10])(int)
(C) void (*(*(*x[10])))(int)
(D) void* (*(x[10]))(*x)(int)
(E) void* (**x)(int)[10]

3.3 Proposed solution
The correct answer is (B) void* (*(*x)[10])(int).

In fact, in the proposed expression x is a pointer to an array of 10 pointers (**x[10]) to a function that takes one int (**(*x[10])(int)) and returns a pointer to void (void* (*(*x[10])(int)).
4 Question 4

4.1 Question

Given the following code, what does the program print?

```c
#include <stdio.h>

void swappiness(int a, int b, int * c, int * d){
    int * e = c;
    c = d;
    d = e;
    int f = a
    a = b;
    b = f;
    f = a;
    a = b;
    b = f;
}

int main(){
    int a = 10, b = 20;
    swappiness(a, b, &b, &a);
    printf("%d %d\n", a, b);
    return 0;
}
```

4.2 Answers

(A) 20 20
(B) 10 20
(C) 20 10
(D) 10 10
(E) Segmentation fault

4.3 Proposed solution

The correct answer is (B) 10 20.

The function `swappiness` just plays around with the variable passed by value (c and d are pointers, but they are still passed by value and never dereferenced) and therefore it has no effect on the variables a and b inside the `main` function.
5 Question 5

5.1 Question
Given the following code, what is the output?

```c
#include <stdio.h>

void knock_knock(char * s){
    while(*s++ != \0)
        printf("Bazinga");
}

int main(){
    int data[5] = {-1, -3, 256, -4, 0};
    knock_knock((char *)data);
    return 0;
}
```

5.2 Answers
(A) BazingaBazingaBazingaBazingaBazingaBazingaBazingaBazinga
(B) BazingaBazingaBazingaBazingaBazingaBazinga
(C) BazingaBazingaBazingaBazingaBazinga
(D) BazingaBazingaBazingaBazingaBazingaBazinga

5.3 Proposed solution
The correct answer is (A) BazingaBazingaBazingaBazingaBazingaBazingaBazingaBazinga.

`data` is an array of int casted to an array of char. Therefore, each one of its elements is addressed byte by byte.
The hex representation of -1 as int is 0xffffffff, thus the function `knock_knock` sees it as four char with value -1.
Analogously, -3 is seen as 0xffffffff (be aware of the endiannes!), i.e. a -3 and three -1, while 256 is seen as 0x00010000, thus its first byte interrupts the while loop, which has iterated 8 times.
6 Question 6

6.1 Question

Given the following code, what is the output?

```c
#include <stdio.h>
#include <stdlib.h>

int main()
{
    int i, *data[10];
    for(i=0; i<10; i++)
        data[i] = malloc(sizeof(int) * 10);
    printf("%ld\n", (long int) (data+3) - (long int) (data + 1));
    return 0;
}
```

6.2 Answers

(A) 4
(B) Cannot tell: the behavior of the program is undefined
(C) 2
(D) 8

6.3 Proposed solution

The correct answer is (D) 8.

**Note:** the question assumes that the program is executed on a 32-bit machine.

Since `data` is an array of pointers and, on a 32-bit machine, the size of a pointer is 4 bytes,

`(long int) (data+3) - (long int) (data + 1)`

is 8, the size of two pointers\(^1\).

\[^1\text{See https://cplusplus.com/doc/tutorial/pointers/#arithmetics; it is a tutorial for C++, but this section is valid also for C} \]

8
7  Question 7

7.1  Question

You are given this simple dynamically-sized linked list implementation. Unfortunately, there's a serious bug: in which function?

typedef struct node_t {
    struct node_t * next;
    int data;
} node_t;

typedef struct linked_list_t {
    node_t * head;
} linked_list_t;

static node_t* new_node() {
    node_t *n = malloc(sizeof(node_t));
    if(n == NULL) exit(1);
    n->next = NULL;
    return n;
}

static linked_list_t* new_linked_list() {
    linked_list_t *list = malloc(sizeof(linked_list_t));
    if(list == NULL) exit(1);
    list->head = NULL;
    return list;
}

static void append_elem(linked_list_t *list, int x) {
    if(list == NULL) exit(1);
    if(list->head == NULL) {
        list->head = new_node();
        list->head->data = x;
    } else {
        node_t *tail = list->head;
        while(tail->next != NULL) tail = tail->next;
        tail->next = new_node();
        tail->next->data = x;
    }
}

void delete_linked_list(linked_list_t *list) {
    node_t *n = list->head;
    while(n != NULL) {
        free(n);
        n = n->next;
    }
}

int main() {
    linked_list_t * l = new_linked_list();
    append_elem(l, 666);
    append_elem(l, 333);
    append_elem(l, 111);
    delete_linked_list(l);
    return 0;
}
7.2 Answers

(A) new_node
(B) new_linked_list
(C) append_elem
(D) delete_linked_list
(E) main

7.3 Proposed solution

The correct answer is (D) delete_linked_list.

In fact, the function delete_linked_list iterates over all the nodes of the list and frees them, but it does not free the pointer to the list itself.
8 Question 8

8.1 Question
Let $y$ be a double in C and let $x = (\text{long})(y + 0.5)$. Which of the following is correct?

8.2 Answers
(A) $x$ is obtained by rounding $y$ to the nearest integer
(B) $x$ is the smallest integer larger than $y$
(C) $x$ is the largest integer smaller than $y$
(D) $x$ is equal to $y$ if and only if $y-0.5$ is integral
(E) $x-y$ is always equal to 0.5

8.3 Proposed solution
The correct answer is (A) $x$ is obtained by rounding $y$ to the nearest integer.

We can write $x = \lfloor y + \frac{1}{2} \rfloor$, so $x$ is equal to a certain value $x'$ if and only if $x' < y < x' + \frac{1}{2}$, i.e. $x' - 0.5 <= y < x' + 0.5$, which is how the rounding to the nearest integer is performed.
9 Question 9

9.1 Question

Given the following code, what is the output?

```c
#include <stdio.h>

int main()
{
    char b = 1;
    while(b <= 127){
        printf("%u\n", (unsigned int) b);
        b++;
    }
    return 0;
}
```

9.2 Answers

(A) 126
(B) 127
(C) 255
(D) Infinite

9.3 Proposed solution

The correct answer is (D) Infinite.

The program prints the value of \( b \) until it is at most 127. But \( b \) is a signed char, thus, when its value is 127 and it is incremented, it becomes -128. Therefore, the loop will never stop and the program will output until it is interrupted.
10 Question 10

10.1 Question

Given the following code, what is the output?

```
#include <stdio.h>

int main(){
    int a = 39, n = 1, k = 0;
    while(a & n){
        k++;
        n *= 2;
    }
    printf("%d", k);
    return 0;
}
```

10.2 Answers

(A) 1  
(B) 2  
(C) 3  
(D) 4  
(E) 5  
(F) 6  
(G) 7  
(H) 8  
(I) 9  
(J) 10

10.3 Proposed solution

The correct answer is (C) 3.

Given the structure of the program, \( n \) is a power of 2 and it is involved in a bitwise AND operation. Therefore it is selecting the bits of \( a \) from the least significant bit to the most significant one, stopping when the first 0 is encountered. Since \( a \) is 39, and 39 in binary is 100111, the while loop iterates 3 times and the value of \( k \) is 3.
11 Question 11

11.1 Question
If you write down all the numbers from 300 to 400, how many times do you have to write the digit 3?

11.2 Answers
(A) 100
(B) 109
(C) 110
(D) 120

11.3 Proposed solution
The correct answer is (D) 120.

The number 400 has no digits equals to 3, so we can exclude it from our reasoning. Every number in the range [300, 399] has the digit 3 as its hundreds digit, which gives us 100 occurrences. Moreover, $\frac{1}{10}$ of the tens digits are 3 and $\frac{1}{10}$ of the units digits are 3, for a total of $100 + 10 + 10 = 120$ occurrences of the digit 3.
12 Question 12

12.1 Question
There are 27 tennis balls. 26 of them have the same weight and the twenty-seventh is a bit heavier. In the worst case scenario, what is the minimum number of weighings you need to identify the heavy one by using a two-pan balance scale?

12.2 Answers
(A) 2
(B) 3
(C) 4
(D) 5
(E) 6

12.3 Proposed solution
The correct answer is (B) 3.

The optimal strategy is to divide the balls into 3 groups, let us say $A, B, C$, and compare two of them with the balance scale. Without loss of generality, we compare the weights of $A$ and $B$. If one of them is heavier than the other, we know that the ball we have to find is in that group. Otherwise, if the two groups have the same weight, the ball is in group $C$.

With this strategy, we restricted the entire set of balls to one third of the initial size. By iterating it, the heaviest ball is identified in 3 weighings.
13 Question 13

13.1 Question

Pedro is a contestant on a “Deal or No Deal” game, and he’s given the choice of three boxes: inside one box is a one million prize, while the others are empty. He picks a box, say No. 1, and the host, who knows what’s inside the boxes, opens another box, say No. 3, which is empty. He then asks him, “Do you want to pick box No. 2 instead?” Is it to his advantage to switch his choice?

13.2 Answers

(A) yes

(B) no

(C) it’s the same

(D) it’s the onion

13.3 Proposed solution

The correct answer is (A) yes.

The answer is yes\(^2\). Ignoring the numbers of the boxes, there are three cases, and each one has probability \(\frac{1}{3}\):

- Pedro chooses the first empty box, the host opens the second one and Pedro wins the prize by switching his choice;
- Pedro chooses the second empty box, the host opens the first one and Pedro wins the prize by switching his choice;
- Pedro chooses the prize, the host opens one of the empty boxes and Pedro wins the money keeping his choice.

In 2 cases over 3 Pedro wins the prize if he change his mind, improving the probability (of \(\frac{1}{3}\)) of choosing the prize at the beginning.

Formally, let us denote by \(P_2\) the event “the prize is inside box No. 2” and by \(E_3\) the event “the box No. 3 is empty”; we can say that \(P(E_3) = \frac{1}{2}\), since Pedro chose box No. 1 and the host has to open one of the two boxes, and \(P(E_3 \mid P_2) = 1\) because the host has to open box No. 3 if the prize is in box No. 2. Now we can exploit Bayes theorem to compute

\[
P(P_2 \mid E_3) = \frac{P(E_3 \mid P_2)P(P_2)}{P(E_3)} = \frac{\frac{1}{3} \cdot \frac{1}{2}}{\frac{1}{2}} = \frac{2}{3}
\]

\(^2\)See https://en.wikipedia.org/wiki/Monty_Hall_problem
14 Question 14

14.1 Question
A director wishes to know how many times her movie has been shown in a given theater. The theater’s staff provides the following info: 1) at the first projection there’s just 1 viewer; 2) at each projection, the number of viewers grows by 1 compared to the previous one; 3) 820 tickets are sold over all the projections. How many projections were held?

14.2 Answers
(A) 13
(B) 20
(C) 40
(D) 81

14.3 Proposed solution
The correct answer is (C) 40.

Let us denote the number of projections of the movie with \( n \). If the number of viewers grows by one each time, the total number of tickets sold will be \( 1 + 2 + 3 + \ldots + n = \sum_{i=1}^{n} i = \frac{n(n+1)}{2} \). Given that 820 tickets are sold, we need to solve for \( n \) the equation \( \frac{n(n+1)}{2} = 820 \), which leads to \( n = 40 \).
15 Question 15

15.1 Question
You can paddle your canoe 7 miles per hour through any placid lake. You’re paddling through the Wabash river and the stream constantly flows at 3 miles per hour. The moment you start to paddle upstream, a fisherman loses one of his fishing bobbers in the water 14 miles upstream of you. How many hours does it take for you to reach the bobber?

15.2 Answers
(A) 1.5
(B) 2
(C) 2.5
(D) 3

15.3 Proposed solution
The correct answer is (B) 2.

Let us pick as reference system the river’s water. Then, your speed is 7 miles per hour, while the water bobber does not move. Since the initial distance is 14 miles, the time needed to reach the bobber is \( \frac{14}{7} = 2 \).
16 Question 16

16.1 Question
A man has 53 socks in his drawer: 21 identical blue, 15 identical black and 17 identical red. The lights are fused and he is completely in the dark. How many socks must he take out to make 100 per cent certain he has a pair of black socks?

16.2 Answers
(A) 21
(B) 36
(C) 40
(D) 48

16.3 Proposed solution
The correct answer is (C) 40.

The worst case is when the man picks all the blue and red socks before picking a pair of black ones. This means that with $21 + 17 + 2 = 40$ socks he will be 100% sure to have a pair of black socks.
17 Question 17

17.1 Question
I’m 5 years older than my sister, who is 7 years younger than Lucy. How old was Lucy when her age was equal to the sum of ours?

17.2 Answers
(A) 2
(B) 7
(C) 9
(D) 10

17.3 Proposed solution
The correct answer is (C) 9.

Let us call with $m$, $s$, $l$ my age, my sister’s one and Lucy’s one respectively. Then we have:

\[
\begin{align*}
    m - s &= 5 \\
    l - s &= 7 \\
    m + s &= l
\end{align*}
\]

that has $(m, s, l) = (7, 2, 9)$ as solution.
18 Question 18

18.1 Question

The Spring Festival is a great occasion for getting to know other people in town, if you know how to dance. Last year, a number of foreigners were traveling by and joined the festival. Each dancer got to perform their favourite dance with their partners. Hans and Linda were fantastic together. Gustavo chose tango, while Javier performed amazingly at the rumba. Lexi watched the waltz, and Ben excelled at the foxtrot. Rebecca danced with Gustavo, while Monica did not dance with Javier. Which dance was picked by Monica?

18.2 Answers

(A) Tango
(B) Foxtrot
(C) Waltz
(D) Rumba

18.3 Proposed solution

The correct answer is (B) Foxtrot.

From the hints, it immediately follows that Gustavo and Rebecca danced the tango, while Ben and Javier danced the foxtrot and the rumba, respectively. It follows that Hans and Linda danced the waltz, since it is the only dance with two free spots for the couple. Since Monica did not dance with Javier, her partner is Ben, thus she danced the foxtrot (and Lexi danced the rumba with Javier).
19 Question 19

19.1 Question
Consider the problem of drawing a square using for each edge either a blue pencil, or a red pencil. How many different squares can we obtain, considering as equal squares obtained from each other by rotation?

19.2 Answers
(A) 4
(B) 6
(C) 8
(D) 10
(E) 12

19.3 Proposed solution
The correct answer is (B) 6.

Let’s divide the problem into cases, looking at how many edges are, for example, red:

- 0 red edges: there is just one configuration;
- 1 red edge: there is one configuration, as all the others can be obtained by a rotation;
- 2 red edges: there are two configurations, one with the red edges that are touching each other and the other one with the red and blue edges that alternate;
- 3 or 4 red edges: this case follow from the cases with 1 and 0 red edges by symmetry, giving one configuration each.

In total, there are $1 + 1 + 2 + 1 + 1 = 6$ different squares.
20 Question 20

20.1 Question

There are 5 houses in 5 different colors, each owned by a person with a different nationality. These owners drink a certain type of beverage, smoke a certain brand of cigar and keep a certain pet. No one has the same pet, smokes the same brand of cigar or drinks the same beverage. Moreover,

1. The Englishman lives in the red house.
2. The Spaniard owns the dog.
3. Coffee is drunk in the green house.
4. The Ukrainian drinks tea.
5. The green house is immediately to the right of the ivory house.
6. The Old Gold smoker owns snails.
7. Kools are smoked in the yellow house.
8. Milk is drunk in the middle house.
10. The man who smokes Chesterfields lives in the house next to the man with the fox.
11. Kools are smoked in the house next to the house where the horse is kept.
12. The Lucky Strike smoker drinks orange juice.
14. The Norwegian lives next to the blue house.

Who owns the zebra?

20.2 Answers

(A) The Norwegian
(B) The Ukrainian
(C) The Japanese
(D) The Englishman

20.3 Proposed solution

The correct answer is (C) The Japanese.

Analyzing the clues, we can reconstruct the entire configuration. For example, by clue 1, clue 5, clue 9 and clue 14, we can deduce that the Norwegian lives in the yellow house (and therefore, by clue 7, the Norwegian smokes Kools).

Using similar reasonings, the following table can be built:

<table>
<thead>
<tr>
<th>House</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Color</td>
<td>Yellow</td>
<td>Blue</td>
<td>Red</td>
<td>Ivory</td>
<td>Green</td>
</tr>
<tr>
<td>Nationality</td>
<td>Norwegian</td>
<td>Ukrainian</td>
<td>Englishman</td>
<td>Spaniard</td>
<td>Japanese</td>
</tr>
<tr>
<td>Drink</td>
<td>Water</td>
<td>Tea</td>
<td>Milk</td>
<td>Orange juice</td>
<td>Coffee</td>
</tr>
<tr>
<td>Smoke</td>
<td>Kools</td>
<td>Chesterfields</td>
<td>Old Gold</td>
<td>Lucky Strike</td>
<td>Parliaments</td>
</tr>
<tr>
<td>Pet</td>
<td>Fox</td>
<td>Horse</td>
<td>Snails</td>
<td>Dog</td>
<td>Zebra</td>
</tr>
</tbody>
</table>

See https://en.wikipedia.org/wiki/Zebra_Puzzle